

# Improving Automated Latent Fingerprint Identification using Extended Minutia Types

Ram P. Krish<sup>a</sup>, Julian Fierrez<sup>b,\*</sup>, Daniel Ramos<sup>b</sup>, Fernando Alonso-Fernandez<sup>c</sup>, Josef Bigun<sup>c</sup>

<sup>a</sup>*School of Electronic Engineering, Dublin City University, Ireland*

<sup>b</sup>*School of Engineering, Universidad Autonoma de Madrid, Spain*

<sup>c</sup>*School of Information Technology, Halmstad University, Sweden*

---

## Abstract

*Latent fingerprints are usually processed with Automated Fingerprint Identification Systems (AFIS) by law enforcement agencies to narrow down possible suspects from a criminal database. AFIS do not commonly use all discriminatory features available in fingerprints but typically use only some types of features automatically extracted by a feature extraction algorithm. In this work, we explore ways to improve rank identification accuracies of AFIS when only a partial latent fingerprint is available. Towards solving this challenge, we propose a method that exploits extended fingerprint features (unusual/rare minutiae) not commonly considered in AFIS. This new method can be combined with any existing minutiae-based matcher. We first compute a similarity score based on least squares between latent and tenprint minutiae points, with rare minutiae features as reference points. Then the similarity score of the reference minutiae-based matcher at hand is modified based on a fitting error from the least square similarity stage. We use a realistic forensic fingerprint casework database in our experiments which contains rare minutiae features obtained from Guardia Civil, the Spanish law enforcement agency. Experiments are conducted using three minutiae-based matchers as a reference, namely: NIST-Bozorth3, VeriFinger-*

---

\*Corresponding author

Email addresses: [ram.krish@dcu.ie](mailto:ram.krish@dcu.ie) (Ram P. Krish), [julian.fierrez@uam.es](mailto:julian.fierrez@uam.es) (Julian Fierrez), [daniel.ramos@uam.es](mailto:daniel.ramos@uam.es) (Daniel Ramos), [feralo@hh.se](mailto:feralo@hh.se) (Fernando Alonso-Fernandez), [josef.bigun@hh.se](mailto:josef.bigun@hh.se) (Josef Bigun)

Accepted Manuscript in Elsevier's Information Fusion

September 27, 2018

© 2018. This manuscript version is made available under the CC-BY-NC-ND 4.0 license.

<http://creativecommons.org/licenses/by-nc-nd/4.0/>

The final version is available online at: <https://doi.org/10.1016/j.inffus.2018.10.001>

*SDK and MCC-SDK. We report significant improvements in the rank identification accuracies when these minutiae matchers are augmented with our proposed algorithm based on rare minutiae features.*

*Keywords:*

Latent Fingerprints, Forensics, Extended Feature Sets, Rare minutiae features

---

## 1. Introduction

Fingerprints left at a crime scene, referred to as latent prints, are the most common type of forensic science evidence and have been used in criminal investigations for more than 100 years, but comparing latent fingerprints is not an easy task. This is mainly attributed to the poor quality of the latent fingerprints obtained from the crime scenes. When a latent fingerprint is found, the criminal investigators first search for the suspect in their criminal database using an Automated Fingerprint Identification System (AFIS) to narrow down their manual work. If there is a match, then the individual is linked to the crime under investigation. Individualization (*identification or match*) is the decision yielded by a forensic examiner about the latent fingerprint belonging to a particular individual. This is the outcome of the Analysis, Comparison, Evaluation and Verification (ACE-V) [1] methodology currently followed in friction ridge examination.

In order to improve the matching efficiency, the concept of “Lights-Out System” was introduced for latent matching [2]. A Lights-Out System is a fully automatic identification process with no human intervention. Here, the system should automatically extract the features from the latent fingerprint and match it against the tenprints (exemplars) stored in the AFIS database to obtain a set of possible suspects with high degree of confidence. In general, latent fingerprints are partial in nature and are of varying quality (see Figure 1), mostly distorted, smudgy, blurred, etc. These factors lead to high number of unreliable extracted features in fully automatic mode, and make it difficult for AFIS to

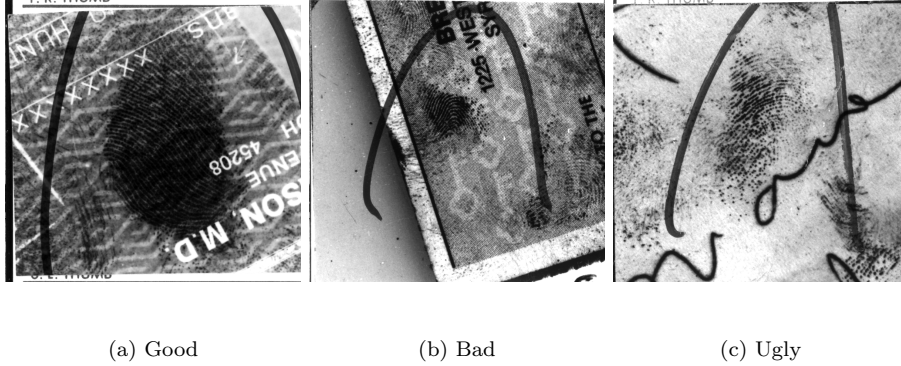


Figure 1: Subjective quality classification of latent fingerprint images in NIST Special Database 27 (NIST-SD27).

perform well. AFIS do not commonly use all the discriminatory features that  
 25 could be derived from a fingerprint, mainly due to the limitations of automatic  
 and reliable extraction of all types of discriminatory features. The accurate  
 performance of feature extraction and matching algorithms of AFIS in forensic  
 scenario is of great importance to avoid erroneous individualization.

Current practice in latent AFIS technology involves marking the latent fin-  
 30 gerprint features manually by forensic examiners and then using both the latent  
 fingerprint image and the manually marked features to search in the AFIS for a  
 list of suspects. Sankaran et al. [3] reviewed existing automated latent finger-  
 print matching algorithms and their limitations. To avoid the burden of manual  
 marking and with the hope of fully automating the latent AFIS in Lights-Out  
 35 mode, the US National Institute of Standards & Technology (NIST) conducted  
 a public evaluation of commercial AFIS performance in Lights-Out mode. This  
 was a multi-phase open project called Evaluation of Latent Fingerprint Tech-  
 nologies (ELFT) [4]. The results of various phases of ELFT are summarized in  
 Table 1. The reported accuracies from Phase-I and Phase-II of ELFT cannot be  
 40 directly compared as the database and the quality of the latents were different.  
 As one of the results of the ELFT initiative [5], it is shown that in some practical  
 conditions manual intervention may be needed, as fully automated procedures

are not yet robust enough, especially when challenging latent fingerprints are considered. The procedures of marking the minutiae, determining the subjective  
45 quality of latents, etc. may need to be carried out manually.

Phase of ELFT	Database size	Rank-1 accuracy
Phase-I [6]	100 latents compared against 10,000 rolled prints	80.0%
Phase-II, Evaluation-1 [7]	835 latents compared against 100,000 rolled prints	97.2%
Phase-II, Evaluation-2 [8]	1,114 latents compared against 100,000 rolled prints	63.4%

Table 1: Summary of NIST Evaluation of Latent Fingerprint Technologies (ELFT) results.

AFIS commonly use only a limited number of features automatically extracted from the fingerprints using a feature extraction algorithm. On the other hand, forensic examiners use a richer set of features during their manual comparisons. This could be a possible reason why manual comparisons outperform  
50 AFIS comparisons [9]. Any features that are not commonly used by commercial AFIS are generally termed as Extended Feature Sets (EFS) [7]. The use of EFS by forensic examiners in manual comparisons is much debated, mainly due to non-repeatability by another examiner to validate the previous decision.

Two major problems in friction ridge analysis that raised the attention of  
55 the forensic community about 10 years ago were identified as follows in [10]:

1. Latent AFIS searches are commonly limited by an over simplified feature set.
2. During the latent examiner comparison, there are no standard format to document the features used in comparison decision. This leads to problems  
60 with future reference or interchange with other forensic examiners.

The SWGFAST (Scientific Working Group on Friction Ridge Analysis, Study, and Technology) drafted a memo to NIST noting that forensic examiners use features that are not currently addressed in fingerprint standards. The ANSI/NIST Standard Workshop II charted the Committee to Define an Extended Fingerprint Feature Set (CDEFFS). The CDEFFS included 45 members from various federal agencies, the forensic community, AFIS vendors, and academia [10]. The purpose of CDEFFS was to define a standard to completely represent the distinctive information in the fingerprint which are quantifiable, repeatable and develop a clear method of characterizing information for: 1) AFIS searches initiated by forensic examiner, and 2) forensic examiner markup and exchange of latent fingerprints.

Fingerprint features are categorized into three levels as well as a feature category called “other” to be used for friction ridge examination. Level-One considers general overall direction of the ridge flow. Level-Two describes the path of specific ridges. Level-Three are the shapes of the ridge structure. “Other” features describe temporary features or imperfections in ridges [11]. Some of the extended fingerprint features defined by CDEFFS under each of the three level categories [10] [12] are summarized in Table 2. Figure 2 shows some extended features and typical minutia features (ridge-endings and bifurcations) in an exemplar fingerprint from NIST Special Database 27 (NIST-SD27).

In this work, we propose a method to improve the identification accuracy of minutiae-based matchers for partial latent fingerprints by incorporating reliably extracted rare minutia features. Most minutiae-based fingerprint matchers use only two prominent ridge characteristics namely *ridge-endings* and *bifurcations*. We propose an algorithm that will modify the similarity scores of minutiae-based matchers based on the presence of rare minutia features like *fragments*, *enclosures*, *dots*, *interruptions*, *etc.* The decision for a match or non-match is automatically estimated based on least squares fitting of an affine transformation between the latent minutiae set and the tenprint minutiae set. We show a significant improvement in the overall rank identification accuracies for three minutiae-based matchers (NIST-Bozorth3, VeriFinger-SDK and

Type of category	Extended feature set
Level-One Details	Ridge flow map, local ridge quality, pattern classification (whorl, arch, tentarch, left/right loop etc), singular points (core, delta), core-delta ridge count.
Level-Two Details	Minutiae-ridge relationship, ridge curvature, feature relationship, unusual/rare minutiae, scars, creases, incipient ridges, dots.
Level-Three Details	Pores, edge shapes, ridge/furrow width.

Table 2: Extended features defined by CDEFFS categorized into respective fingerprint feature details (not a comprehensive list).

MCC-SDK) when their similarity scores are modified using our proposed algorithm which incorporates rare minutia features. A preliminary version of this work [13] modifies the scores based on the probability of occurrence of rare  
95 minutiae features. Here, we propose a method which avoids dependencies on such probability of occurrence as they may vary depending on the size of the database.

The main contributions of this work are as follows:

1. A methodology to adapt any minutiae-based matcher by incorporating  
100 information from rare features.
2. A specific algorithm to align the latent minutiae pattern and the tenprint minutiae pattern using rare minutiae.
3. Experimental demonstration of the performance improvement of minutiae-based matchers when incorporating information from rare features.
- 105 4. We finally present also various population statistics about rare minutia features present in a realistic forensic casework database obtained from Spanish law enforcement agency (Guardia Civil).

In the following sections, we review related works in the individualization of

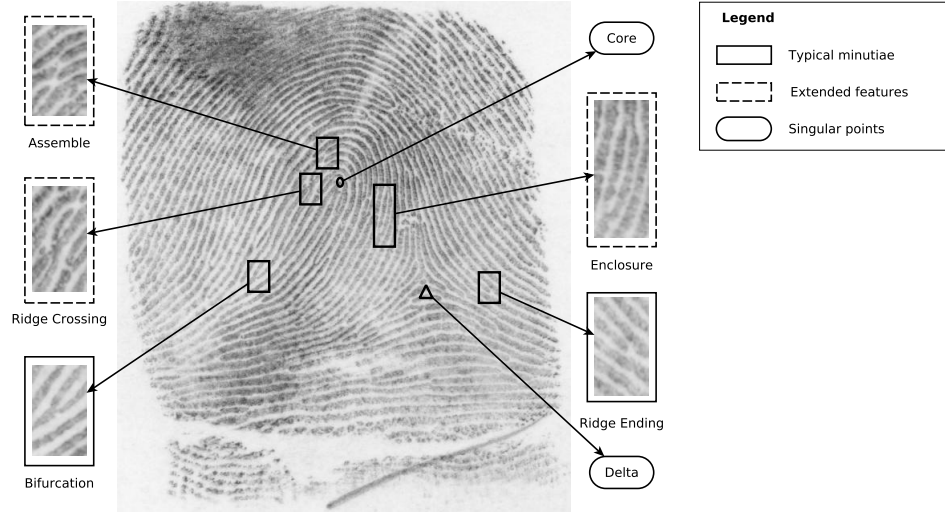


Figure 2: Typical minutiae (ridge-ending, bifurcation), extended features (assemble, ridge-crossing, enclosure) and singular points (core, delta) in an exemplar fingerprint from NIST-SD27 database.

fingerprints, and describe: the database and statistics of rare minutia features,  
the proposed algorithm to modify the similarity scores based on rare features,  
experiments, results and conclusions.

## 2. Related works

To use EFS in automated systems, reliable feature extraction algorithms are mandatory. Many law enforcement agencies follow a 500 ppi scanning resolution  
for fingerprint images to be used in AFIS. With such a resolution, it is difficult to  
reliably extract many of the extended features automatically. Due to advances  
in fingerprint scanning technologies, SWGFAST during the ANSI/NIST Finger-  
print Standard Update Workshop in 2005 proposed 1000 ppi as the minimum  
scanning resolution for fingerprint images. This proposal was hugely supported  
by the forensic community. To test the feasibility of including EFS in latent  
AFIS, NIST conducted another multi-phase commercial algorithm evaluation  
called Evaluation of Latent Fingerprint Technologies - Extended Feature Sets

<b>ELFT-EFS</b>	<b>Database size</b>	<b>Rank-1 accuracy</b>
Evaluation-1 [14]	1,114 latents compared against 1,000,000 rolled prints and 1,000,000 plain prints	66.7%
Evaluation-2 [15] [16]	1,066 latents compared against 1,000,000 rolled prints and 1,000,000 plain prints	71.4%

Table 3: Rank-1 identification accuracy of NIST Evaluation of Latent Fingerprint Technologies - Extended Feature Sets (ELFT-EFS).

(ELFT-EFS) [14].

ELFT-EFS was conducted in a “Semi Lights-Out” mode, unlike the “Lights-Out” mode for ELFT. The main purpose of ELFT-EFS was to determine the effectiveness of forensic examiner marked latent fingerprint features on the latent identification accuracy. NIST conducted two evaluations for ELFT-EFS and the best achieved Rank-1 identification accuracy for each of the evaluations is summarized in Table 3.

As in ELFT, the results of different evaluations in ELFT-EFS cannot be directly compared because the database used were not exactly the same [15] [14]. In [15], it is reported that though the highest measured accuracy achieved by a individual matcher at Rank-1 was 71.4%, and approximately 82% of the latents were correctly matched at Rank-1 when multiple matchers were combined. This corroborates the potential for additional accuracy improvement when combining multiple algorithms [17]. Nevertheless, these NIST evaluations show that the performance of state of the art latent fingerprint recognition technologies are not satisfactory.

An extensive study on extended fingerprint feature sets is reported by Jain [9]. This includes several extended features from Level-One, Level-Two and Level-Three. It was concluded in [9] that manual intervention is strongly recommended



while using EFS, as well as extended features from Level-One and Level-Two are highly recommended to be incorporated in latent AFIS. Extended features such as ridge flow map, ridge wavelength map, ridge quality map, and ridge skeleton  
145 have shown significant improvements in latent identification accuracies. Level-One and Level-Two details used in [9] [18] are insensitive to image quality, and do not rely on high resolution images. To incorporate Level-Three EFS such as pores, dots, incipients, etc, it is essential to improve the quality of enrolled fingerprints.

150 The use of pores as extended features was studied in high resolution 1000 ppi images by Zhao et al. [19] and Jain et al. [20]. Dots and incipients were studied by Chen et al. [21]. Out of pores, dots and incipients, pores resulted in better performance [19]. Even though high resolution 1000 ppi images were used, live scan images resulted in easy detection of pores automatically, which was not  
155 the case with inked fingerprint images. Pore extraction based on skeletonized and binary images was studied by Stosz et al. [22, 23] and Kryszczuk et al. [24]. These techniques were demonstrated effective only on very good quality high resolution fingerprint images scanned approximately at 2000 ppi [22]. These methods were more sensitive to noise, and the performance degrades for poor  
160 quality of fingerprint images and low resolution images.

A local image quality based method applied on extended fingerprint features for high resolution 1000 ppi fingerprint images was reported by Vatsa et al. [25]. A fast curve evolution algorithm was used to quickly extract extended features such as pores, ridge contours, dots and incipient ridges. Together with other  
165 Level-One and Level-Two details as proposed in Jain et al. [18], these extended features were used to generate a quality-based likelihood ratio to improve the identification performance.

Score level fusion of different algorithms using various extended fingerprint features was reported by Fierrez et al. [26]. Features like singular points, ridge  
170 skeleton, ridge counts, ridge flow map, ridge wavelength map, texture measures were studied by analyzing the correlation between them using feature subset-selection techniques. Combination of features showed significant improvement

in the performance of the system.

When only partial fingerprints are available, pre-alignment of partial minutiae set and full minutiae set based on orientation fields of respective fingerprints helps in reducing the minutiae search space of full fingerprint relative to the size of partial fingerprint. Such reduction in the size of minutiae search space has been shown to improve the performance by Krish et al. [27], [28], [29]. This approach has shown significant improvement in the system performance especially for poor quality latent fingerprints.

Si et al. [30] combined local and global approaches for minutiae matching. Their proposed method estimates a dense deformation field between two fingerprints to remove the negative impact of distortion. The dense deformation field aligns not only minutiae but also ridges. By fusing minutiae and image correlation, they improved the matching performance significantly.

Cao and Jain [31] proposed the use of minutiae descriptors that are learned via a ConvNet together with minutiae and texture information to improve the latent fingerprint recognition. They performed score level fusion of their proposed algorithm with commercial minutiae-based matchers to improve the rank identification accuracies. We followed a similar methodology to show the importance of rare minutiae features in improving the rank identification accuracies of minutiae-based matchers.

### 3. Database

Similar to the related works discussed in Sect. 1, we first tried to use SD27 data from NIST in our experiments. Regretfully, the public distribution of SD27 data from NIST is now discontinued. Additionally, copies already distributed of SD27 lack ground truth information of the existing rare features, therefore we decided to generate and make public a new dataset similar to SD27 but in this case including ground truth information generated by forensic experts.<sup>1</sup>

---

<sup>1</sup>The dataset is available here: [https://atvs.ii.uam.es/atvs/gcdb\\_features.html](https://atvs.ii.uam.es/atvs/gcdb_features.html)

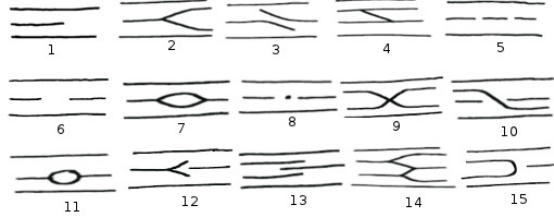


Figure 3: Minutia types used by Guardia Civil. Names corresponding to individual minutia type numbers can be found in Table 4.

200 The database used in this work was obtained from Guardia Civil, the Spanish law enforcement agency. The Guardia Civil database (GCDB) is a realistic forensic fingerprint casework database. Apart from having typical minutiae feature types (*ridge-endings*, *bifurcations*), GCDB also comprises rare minutiae types like *fragments*, *enclosures*, *dots*, *interruptions*, etc [32]. A comprehensive  
205 list of rare minutia features used by Guardia Civil are shown in Figure 3 and the corresponding minutiae type names are listed in Table 4.

GCDB used in this work consists of 268 latent and tenprint (exemplar) pairs of fingerprint images (scanned at 500 ppi) and minutia sets. All the minutiae in the latent fingerprint images were manually extracted by forensic examiners  
210 of Guardia Civil. The corresponding mated minutiae in the tenprints were also manually established. This includes the typical (ridge-endings and bifurcations) minutiae and the rare minutiae. These are called *matched* minutiae set, i.e, the minutiae sets for which a one-to-one correspondence is established between the latent and the mated tenprint. Here, the number of minutiae in the latent and  
215 the corresponding mated tenprint minutiae set are the same.

To generate an *ideal* minutiae set (i.e, all possible minutiae) for the tenprint, we used the minutiae extractor module from VeriFinger-SDK [33]. We performed a Gabor filtering based global post-processing to remove any spurious minutiae that are outside the foreground. In particular, Gabor filtering  
220 is used to obtain the Region of Interest (RoI) similarly to [34]. The spurious minutiae generated by VeriFinger outside the RoI are then eliminated. Ver-

No	Minutiae type	No	Minutiae type	No	Minutiae type
1	Ridge Ending	6	Interruption	11	Circle
2	Bifurcation	7	Enclosure	12	Delta
3	Deviation	8	Point	13	Assemble
4	Bridge	9	Ridge Crossing	14	M-structure
5	Fragment	10	Transversal	15	Return

Table 4: List of minutia types used by Guardia Civil. Numbering with respect to Figure 3.

iFinger extracts only the typical minutiae features from the fingerprint image. We then added the rare minutiae from the GCDB tenprint minutiae set into the post-processed VeriFinger generated minutiae set for the tenprints. In this case the number of minutiae between the latent and the corresponding mated  
225 tenprint minutiae set are not equal, the latent minutiae set is only a subset of the tenprint minutiae set. The average number of minutiae in the latents was 13 and that of tenprints was 125. There exists automated algorithms to perform segmentation for latent fingerprints [35], but in this work, we relied on  
230 the manually extracted minutiae alone.

The original latent minutia sets provided by Guardia Civil and the post-processed VeriFinger generated minutia sets are used in all our experiments. To represent some rare minutiae, multiple points were needed. For example, to represent a *deviation* two points are needed (see type 3 in Figure 3), and  
235 to represent an *assemble* three points are needed (see type 13 in Figure 3). Whenever multiple points are needed to represent a rare minutia, we mapped them to a single point representation by taking the average of locations of all points, and minimum orientation among all the orientations.

From the 268 latent fingerprint minutia sets, we estimated the probability of occurrence ( $p_i$ ) of various minutia types. The probability ( $p_i$ ) for each minutia  
240 type present in GCDB is listed in Table 5. In the 268 latent fingerprints of GCDB, we noticed only seven types of rare minutia features. They are listed in

No	Minutiae Type	Probability ( $p_i$ )	Number of occurrences
1	Ridge-ending	0.5634	1902
2	Bifurcation	0.3620	1222
3	Deviation	0.0015	5
4	Bridge	0.0024	8
5	Fragment	0.0444	150
6	Interruption	0.0021	7
7	Enclosure	0.0204	69
8	Point	0.0036	12
10	Transversal	0.0003	1

Table 5: The probability of occurrence of minutia types present in the 268 latent fingerprints of GCDB (total number of minutiae observed = 3376). The numbers correspond to minutia types in Figure 3

Table 5. Other rare minutia types are not found in the current database used in this study. This is particularly due to the fact that we are dealing with highly partial latent fingerprints, with an average of 13 minutiae per latent.

In related works, minutiae frequency for 20 different minutiae types were reported for full fingerprints obtained from a population of 200 Spanish individuals [36] and 278 Argentinian individuals [37]. The statistics of the various minutiae types obtained in those works (for ca. 2,000 different fingerprints, more than 80,000 minutiae) are similar in many cases to the statistics obtained in the partial latent fingerprint database presented in the present work if we compare corresponding types of features, especially for the most frequent minutiae types. For the comparison, please note that the naming conventions differ among works. Here we follow the naming conventions of Guardia Civil, e.g.,

255 Type 6 in Fig. 3 is called “Interruption”, whereas this kind of feature is called  
“Break (BR)” in works [36] and [37]. Comparing for example our statistics from  
Table 5 to Table 1 of [36], and using approximated values, our Type 1 is 56% vs  
Type E in [36] is 50%, our Type 2 is 36% vs Type B+C is 40%, our Type 7 is  
2% vs Type ENBG+ENSM is 2%, etc. A few other types, specially the rarest,  
260 have larger differences in their statistics, most probably because of the sample  
size, e.g., our Type 3 is ca. 0.1% vs Type O in [36] is 0.7%.

Given our limited sample size, please note that the statistics from Table 5  
are not pretending to be representative of large-scale populations, especially for  
the rarest features. It would be necessary a really large dataset to generate  
265 statistically significant frequencies for all the reported types, which is out of the  
scope of the present paper.

#### 4. Algorithm

We assume in our algorithm that the rare features won’t be always repeatable  
and won’t be always labelled uniformly over multiple captures (either manually  
270 or automatically), e.g., due to acquisition variations or other image quality  
factors [38, 39]. Similarly to minutiae matchers able to cope with variations  
between matching fingerprint images, our algorithm is also able to cope with  
such intra-variability. A comprehensive study of such variability factors is out  
of the scope of the present work. Here we only focus in analyzing to what  
275 extent those rare minutiae can improve existing AFIS, using realistic data in  
which such intra-variations between multiple captures are naturally present.  
The latent fingerprints of GCDB are highly partial in nature, with an average  
of 13 minutiae per latent. To make an appropriate alignment between the latent  
minutia points and the tenprint minutia points (with an average of 125 minutia  
280 points) requires a reliable reference point. We choose the rare minutia features  
as reference points to perform the alignment.

Let  $L$  and  $M$  be the representation of latent and tenprint minutia sets re-  
spectively. Each minutia is represented as a quadruple  $m = \{x, y, \theta, t\}$  that

indicates the  $(x, y)$  location as coordinates, the minutia angle  $\theta$  and the minutia type  $t$ :

$$L = [m_1 \ m_2 \ \dots \ m_p], \quad m_i = [x_i \ y_i \ \theta_i \ t_i]^T, \quad i = 1 \dots p$$

$$M = [m'_1 \ m'_2 \ \dots \ m'_q], \quad m'_j = [x'_j \ y'_j \ \theta'_j \ t'_j]^T, \quad j = 1 \dots q,$$

where  $p$  and  $q$  are the number of minutiae in  $L$  and  $M$  respectively. If  $t > 2$ , then the minutia is of rare type (from Table 4), and  $[\cdot]^T$  denotes transpose.

The algorithm to generate weighted similarity scores from a minutiae matcher is described in two stages. Similarity scores of minutiae matchers are modified only if they contain rare minutia features.

The first stage of the algorithm estimates the least square fitting error for an affine transformation of the latent minutiae set onto a tenprint minutiae set. The second stage of the algorithm modifies the similarity score generated by the minutiae-based matcher based on the fitting error. Other works related with modifying the similarity score based on pre-alignment are reported in [40, 27, 41]. The sequence of steps involved in generating the modified score of the minutiae matcher using our proposed algorithm is summarized in Figure 4.

### ***Stage-1 : Least Square Fitting Error***

**Step 1:** To find the affine transformation between  $L$  and  $M$ , it is first needed to establish a one-to-one correspondence between minutiae from  $L$  and minutiae from  $M$ . Let the subset of minutiae from  $M$  which establishes correspondence with  $L$  be denoted as  $M_s$ .

**Step 2:** Superimpose one rare minutia point of  $L$  onto the corresponding rare minutia point of  $M$ , only if they both are of the same type (if there are multiple rare minutia points, take any). This step compensates the translation between latent and tenprint. If the type of the rare minutia between  $L$  and  $M$  differs, or  $M$  does not contain any rare minutiae, then the similarity score generated by our algorithm is fixed to a value 0.25 inside a range (0,1). That similarity score will then be combined with the score provided by the AFIS system (see Figure 4). Note that we align based on rare minutiae of the same

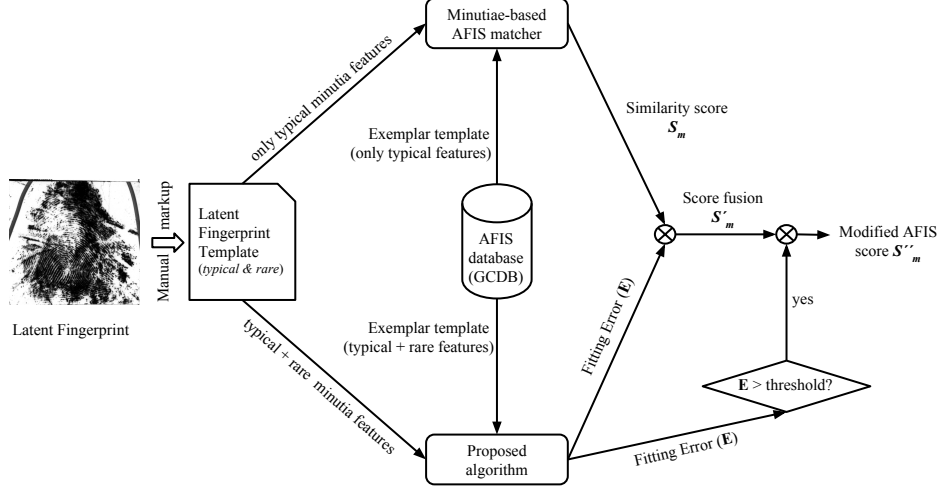


Figure 4: Sequence of steps in estimating the modified similarity score of a reference minutiae-based matcher. Note that the AFIS matcher that we want to improve runs in parallel and independently of our proposed algorithm based on rare features. Our proposed algorithm generates a new score that is fused to the standard output score provided by the AFIS matcher.

type between latent and tenprint. Provided that rare minutia are more unique than standard minutia and that the baseline AFIS that we are trying to improve most probably won't be exploiting such specific rare types, we expect that our combination approach shown in Figure 4 will fuse complementary information resulting in improved performance.

**Step 3:** To establish the correspondence between latent and tenprint minutia points, we choose the minutia points from  $M$  that are close to the minutia points of  $L$ . The Euclidean distance is calculated between the minutia pairs to determine whether the pairs are close or not.

**Step 4:** To compensate for rotation alignment, we rotate the latent in the range  $[-45^\circ, +45^\circ]$  with respect to the superimposed rare minutiae, and estimate the Euclidean distance for each rotation step of size  $1^\circ$ .

**Step 5:** The optimal rotation is the one for which the average sum of distances between closest pairs is minimum.



**Step 6:** After the alignment, all those minutia pairs which are within a threshold distance are considered to be mated pairs, and a one-to-one correspondence is established between them. As a result, we obtain a subset  $M_s$  of the tenprint minutiae  $M$ . After establishing the correspondence, the number of  
325 minutiae between  $L$  and  $M_s$  are the same.

**Step 7:** Once the correspondence is established, we find the least square fitting error for the affine transformation between the latent minutia points and the subset of tenprint minutiae set.

For  $\hat{L}$  and  $\hat{M}_s$ , which are the modified version of  $L$  and  $M_s$  with only the  
330  $(x, y)$  locations as minutia representation augmented with a value 1, i.e.,

$$\begin{aligned}\hat{L} &= [\hat{m}_1 \ \hat{m}_2 \ \dots \ \hat{m}_p]; \quad \hat{m}_i = [x_i \ y_i \ 1]^T; \quad i = 1 \dots p \\ \hat{M}_s &= [\hat{m}'_1 \ \hat{m}'_2 \ \dots \ \hat{m}'_p]; \quad \hat{m}'_j = [x'_j \ y'_j \ 1]^T; \quad j = 1 \dots p,\end{aligned}$$

we are looking for some affine transformation matrix

$$A = [a_{jk}]_{j,k=1 \dots 3} \quad (1)$$

and some translation vector

$$\tau = [\tau_1 \ \tau_2 \ \dots \ \tau_p]; \quad \tau_1 = \tau_2 = \dots = \tau_p = [\delta_x \ \delta_y \ 1]^T; \quad (2)$$

such that

$$\hat{M}_s \approx A\hat{L} + \tau \quad (3)$$

where  $[\delta_x \ \delta_y]$  is the translation needed to superimpose the rare minutia of latent minutia set  $L$  and tenprint minutia set  $M$ .

**Step 8:** Find the least square fitting error between  $\hat{L}$  and  $\hat{M}_s$  defined as follows:

$$E^{\hat{L}, \hat{M}_s} = \frac{1}{p} \sum_{i=1}^p \|\hat{m}'_i - A\hat{m}_i - \tau_i\|_2^2 \quad (4)$$

where  $\|\hat{m}'_i - A\hat{m}_i - \tau_i\|_2$  is the  $L_2$  norm.

335 For a match comparison, we expect this fitting error to be small, whereas  
for a non-match comparison, the fitting error is expected to be large.

If there are multiple matching rare minutiae feature between  $L$  and  $M_s$ ,  
then  $E^{\hat{L}, \hat{M}_s}$  is calculated for all such minutiae types. The fitting error for such  
a comparison is chosen to be the minimum of all the fitting errors calculated.

#### 340 **Stage-2 : Modified scores**

**Step 9:** Using a standard minutia matcher, generate the similarity score  $S_m$   
between  $L$  and  $M$ . Assuming that the similarity score values generated by the  
minutiae matcher is normalized in range  $[0, 1]$ . If by default the minutiae-based  
matcher do not generate normalized scores, then they are explicitly normalized.

345 The fitting error  $E^{\hat{L}, \hat{M}_s}$  is a dissimilarity score, i.e, lower the fitting error,  
comparison is more similar. The fitting error is normalized in the range  $[0, 1]$   
and then they are converted into a similarity score  $\hat{E}^{\hat{L}, \hat{M}_s}$  as follows:

$$\hat{E}^{\hat{L}, \hat{M}_s} = 1 - E^{\hat{L}, \hat{M}_s} \quad (5)$$

$S_m$  and  $\hat{E}^{\hat{L}, \hat{M}_s}$  are similarity scores in the range  $[0, 1]$ . First level of score  
modification is done by score fusion of  $S_m$  and  $\hat{E}^{\hat{L}, \hat{M}_s}$  based on mean rule to  
350 obtain  $S'_m$  as follows:

$$S'_m = \frac{S_m + \hat{E}^{\hat{L}, \hat{M}_s}}{2} \quad (6)$$

**Step 10:** Further to the score modification based on fusion, similarity score  
 $S'_m$  is again modified based on a fitting error threshold  $E_t$  to obtain  $S''_m$  as  
follows:

$$S''_m = \begin{cases} S'_m \times \alpha & \text{if } \hat{E}^{\hat{L}, \hat{M}_s} > E_t, \\ S'_m \times \beta & \text{otherwise.} \end{cases} \quad (7)$$

where  $\alpha$  and  $\beta$  are constants used to reward and penalize the fused score  $S'_m$   
355 respectively.

If  $\hat{E}^{\hat{L}, \hat{M}_s} > E_t$ , then the comparison is deemed to be a match, and the fused score is further rewarded by multiplying with a constant  $\alpha$  to obtain  $S''_m$ . If  $\hat{E}^{\hat{L}, \hat{M}_s} \leq E_t$ , the comparison is deemed to be a non-match, and the fused score  $S'_m$  is penalized by multiplying it with constant  $\beta$  to obtain  $S''_m$ .

360 Thus, we obtain a modified similarity scores  $S''_m$  for a particular minutiae matcher by incorporating information from rare minutia features based on the fitting error obtained using our approach.

## 5. Experiments

GCDB consists of 268 latent and corresponding 268 mated tenprint images  
365 and minutiae. Only 151 of them contains rare minutiae in the minutiae set, and the remaining consisted only of bifurcations and ridge-endings. We performed all our experiments on the 151 latent and tenprint minutiae set to establish the importance of rare minutiae using our proposed algorithm in improving the rank identification accuracy of minutiae-based matchers which uses only typical  
370 minutiae. To generate similarity scores based on typical minutia features, we used three minutiae matchers namely: NIST-Bozorth3 [42], VeriFinger-SDK [33] and MCC-SDK [43, 44, 45]. When reporting the rank identification accuracies in our experiments, there are 151 match comparisons and  $151 \times 150$  non-match comparisons.

375 NIST-Bozorth3 is a minutiae based fingerprint matcher that is specially developed to deal with latent fingerprints and is publicly available. This matcher is part of the NIST Biometric Image Software (NBIS) [42], developed by NIST. VeriFinger is a commercial SDK that is widely used in academic research. MCC-SDK is a well known minutiae matcher made available for research purposes.  
380 Both NIST-Bozorth3 and MCC-SDK are publicly available minutiae matchers, whereas VeriFinger is not. We report the performance accuracy and improvement of all the matchers using Cumulative Match Characteristic (CMC) curves.

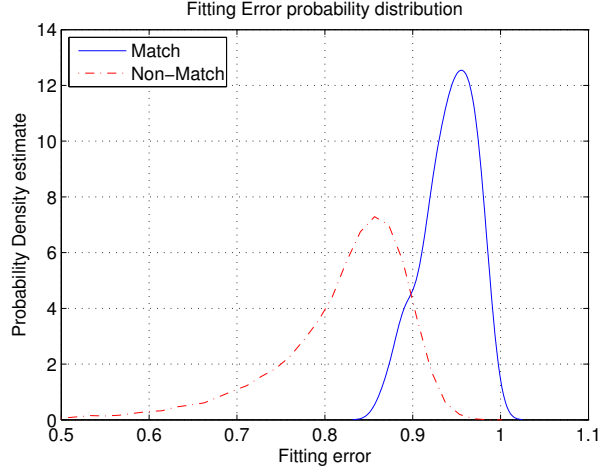


Figure 5: Probability density estimate of the fitting errors for match and non-match comparisons.

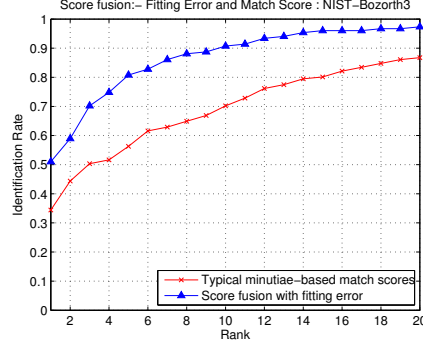
#### 5.1. Experiment 1: Fitting Error probability distribution

The least square fitting error probability density estimates for both match  
 385 and non-match comparisons are shown in Figure 5. We can observe that the fitting error itself is discriminatory enough, having separate peaks for both match and non-match distributions. This supports the methodology followed in our algorithm. The following experiments also support this fact.

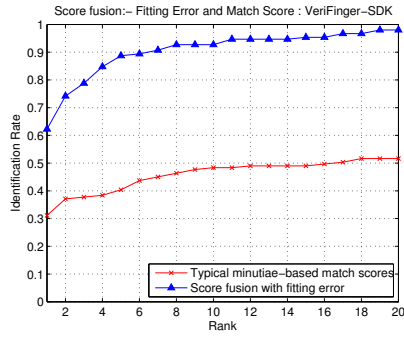
#### 5.2. Experiment 2: Score Fusion

390 The fitting error is a similarity score in the range  $[0, 1]$  from Eq. (5). The similarity scores obtained from minutiae-based matchers are normalized in the range  $[0, 1]$ . These scores are fused based on sum rule (Step 9 of Algorithm).

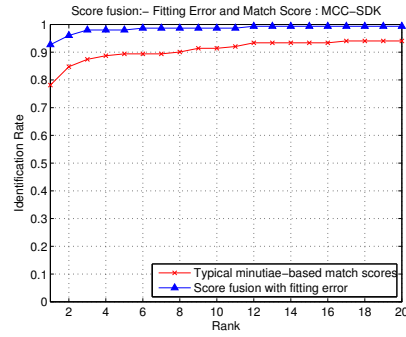
Figures 6(a), 6(b) and 6(c) show the CMC curve before and after score fusion for minutiae-based matchers NIST-Bozorth3, VeriFinger-SDK and MCC-  
 395 SDK respectively. Typical minutiae-based similarity scores were very poor for NIST-Bozorth3 and VeriFinger-SDK at Rank-1 identification and beyond. NIST-Bozorth3 achieved only 34.44% Rank-1 identification accuracy when only typical minutiae (ridge-endings and bifurcations) were used. VeriFinger-SDK achieved 31.13% Rank-1 identification accuracy under similar configuration.



(a) CMC curve for NIST-Bozorth3 before and after score fusion



(b) CMC curve for VeriFinger-SDK before and after score fusion



(c) CMC curve for MCC-SDK before and after score fusion

Figure 6: CMC curve showing consistent improvement in the rank identification accuracies for NIST-Bozorth3, VeriFinger-SDK and MCC-SDK when their minutiae-based similarity scores are fused with fitting error based on the rare minutiae proposed in our algorithm.

400 The performance of MCC-SDK is far better than other two matchers, and achieved 78.15% Rank-1 identification accuracy when only using typical minutiae. In general, MCC-SDK is one of the best performing local structure based minutiae matcher.

The similarity score  $S_m$  of the minutiae-based matcher is modified by fusing

Matcher	Before score fusion (Rank-1)	After score fusion (Rank-1)
NIST-Bozorth3	34.44	51.00
VeriFinger-SDK	31.13	62.25
MCC-SDK	78.15	92.72

Table 6: Rank-1 identification (in %) for NIST-Bozorth3, VeriFinger-SDK and MCC-SDK before and after score fusion.

405 with the fitting error  $\hat{E}^{\hat{L}, \hat{M}_s}$  using mean rule to obtain  $S'_m$  (Eq. (6)). This score fusion significantly improves the rank identification accuracies for all minutiae-based matchers. The Rank-1 identification improved from 34.44% to 51.00% for NIST-Bozorth3, 31.13% to 62.25% for VeriFinger-SDK, and 78.15% to 92.72% for MCC-SDK. The improvement obtained at this stage is significant and consistent at all the ranks (Figures 6(a), 6(b) and 6(c)).

Table 6 summarizes the Rank-1 accuracy for NIST-Bozorth3, VeriFinger-SDK and MCC-SDK before and after score fusion with fitting error obtained using our proposed method.

### 5.3. Experiment 3: Score modification based on fitting error threshold

415 The fitting error threshold  $E_t$  plays a crucial factor in our proposed algorithm. Based on the fitting error, a given comparison can be concluded whether it is a match comparison or a non-match comparison. If the fitting error  $\hat{E}^{\hat{L}, \hat{M}_s}$  is greater than a threshold  $E_t$ , then the comparison is concluded a match comparison. This is because  $\hat{E}^{\hat{L}, \hat{M}_s}$  is also viewed as a similarity measure. When the comparison is deemed to be a match comparison based on threshold  $E_t$ , then 420 the fused score  $S'_m$  is rewarded by multiplying with a constant  $\alpha$ . Similarly, when the comparison is deemed as non-match, then fused score  $S'_m$  is penalized by multiplying with a constant  $\beta$ . In our experiments, we empirically chose  $\alpha = 2$  and  $\beta = 1$  (Step 10 of Algorithm, Eq.(7)).

425 Figures 7(a), 7(c) and 7(e) show Rank-1 identification accuracies (Y-axis) obtained for various fitting error thresholds (X-axis) for NIST-Bozorth3, VeriFinger-

Matcher	Before score fusion (Rank-1)	After score fusion (Rank-1)	Threshold based modification (Rank-1)
NIST-Bozorth3	34.44	51.00	74.83
VeriFinger-SDK	31.13	62.25	77.48
MCC-SDK	78.15	92.72	96.03

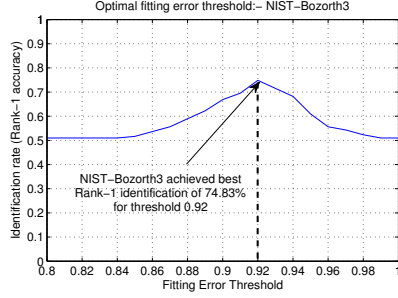
Table 7: Rank-1 identification (in %) for NIST-Bozorth3, VeriFinger-SDK and MCC-SDK when the fused scores are modified based on fitting error threshold. Results are reported on the subset of mated latent-tenprint pairs where rare features are found (151 out of 268 pairs).

SDK and MCC-SDK respectively. The threshold is varied in the range 0.8 to 1.0, as most of the fitting error similarity values are concentrated in this range (see Figure 5). The best fitting error threshold for each of the matchers are obtained  
430 heuristically. Same database is used for both this heuristic estimation as well reporting the performance improvement of the systems. This is particularly due to the objective of looking for best possible performance the system can achieve as compared to only score fusion. Consequently, this also helps to understand the discriminating capability of the fitting error, supporting Figure 5.

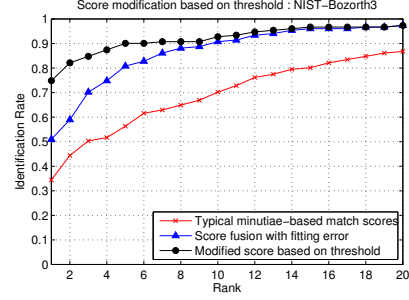
435 For NIST-Bozorth3, we notice that for a threshold value of 0.92 (see Figure 7(a)), the system achieves 74.83% Rank-1 identification accuracy. Using our proposed algorithm, we were able to significantly improve the Rank-1 identification accuracy of NIST-Bozorth3 from 34.44% to 74.83%. Figure 7(b) show the CMC curve for NIST-Bozorth3 when the fused scores are modified based on the  
440 fitting error threshold. We observe a significant and consistent improvement of rank identification accuracies for NIST-Bozorth3.

Figure 7(d) show the CMC curve based on optimal threshold for VeriFinger-SDK. For the optimal threshold value of 0.93 (see Figure 7(c)), VeriFinger-SDK achieved Rank-1 identification accuracy of 77.48% which is a significant im-  
445 provement from 31.13%. We also observe that, using our proposed algorithm, we achieve significant and consistent improvement in rank identification accuracy for VeriFinger-SDK when the rare minutiae information is incorporated.

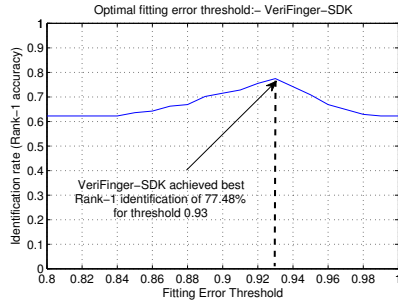
Similarly, Figure 7(f) show the best CMC curve for MCC-SDK. For an op-



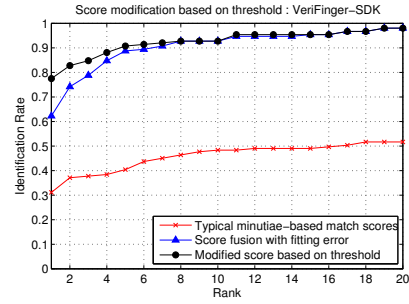
(a) Looking for optimal threshold based on Rank-1 identification accuracy for NIST-Bozorth3.



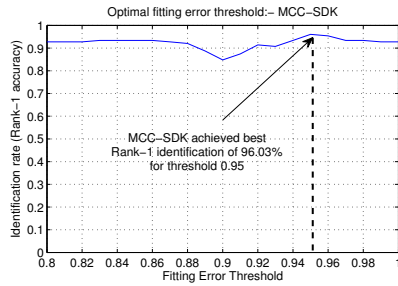
(b) CMC curve for NIST-Bozorth3 after modifying the fused score based on fitting error threshold.



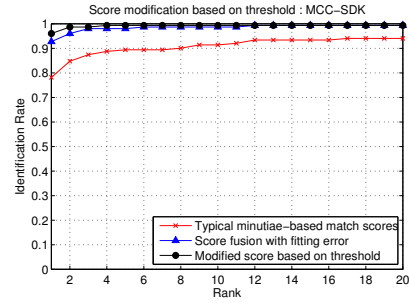
(c) Looking for optimal threshold based on Rank-1 identification accuracy for VeriFinger-SDK.



(d) CMC curve for VeriFinger-SDK after modifying the fused score based on fitting error threshold.



(e) Looking for optimal threshold based on Rank-1 identification accuracy for MCC-SDK.



(f) CMC curve for MCC-SDK after modifying the fused score based on fitting error threshold.

Figure 7: CMC curve showing consistent improvement in the rank identification accuracies for NIST-Bozorth3, VeriFinger-SDK and MCC-SDK when the fused scores are further modified based on fitting error threshold. Left column show the parameter optimization by looking for optimal threshold. Right column show the improvement in rank identification after applying optimal threshold.



Matcher	Baseline AFIS (Rank-1)	Improved Matcher (Rank-1)
NIST-Bozorth3	25.37	36.94
VeriFinger-SDK	31.72	59.33
MCC-SDK	80.60	89.93

Table 8: Rank-1 identification (in %) for the 3 considered baseline fingerprint matchers before and after applying the proposed improvement based on rare features, on the full set of 268 latent-tenprint pairs included in GCDB database.

timal threshold value of 0.95 (see Figure 7(e)), MCC-SDK achieved the best Rank-1 identification of 96.03%, as well as consistent improvement in rank identification using our proposed algorithm. Table 7 summarizes the Rank-1 identification for all the minutiae-based matchers used in our experiments on the subset of mated latent-tenprint pairs where rare features are found (151 out of 268 pairs). Table 8 finally shows the performance over the full set of 268 latent-tenprint pairs, in which 151 out of them (the set that includes rare features) are benefited from our proposed algorithm as indicated in Table 7, and the remaining 117 are processed only with the baseline AFIS under consideration (i.e., the similarity score  $S_m$  in Figure 4 is the only one used).

## 6. Conclusions

We discussed the challenges faced by latent fingerprint identification. One of the crucial challenges faced by AFIS is on how to improve the rank identification accuracies when only partial fingerprints are available. We proposed an algorithm that incorporates information from reliably extracted rare minutia features to improve the rank identification accuracies for minutiae matchers.

The usefulness of the proposed algorithm is demonstrated on three widely used minutiae-based matchers, NIST-Bozorth3, VeriFinger-SDK and MCC-SDK. All the three matchers showed significant improvement in the rank identification accuracies when their similarity scores were modified based on the fitting error proposed in our methodology. We conclude that even if we have only few

470 number of minutiae in a partial latent, presence of reliably extracted rare minutiae features makes the comparison more robust. In our experiments, we used the rare minutiae features that were manually extracted by forensic examiners. Developing more robust automatic extraction of rare minutiae can significantly improve the current state of the art in AFIS adapted for latent fingerprints.

475 Also, future work may exploit the differences between minutiae types to further improve the performance of standard AFIS, e.g., by incorporating weighting factors in the alignment or matching steps [46] when combining those AFIS with auxiliary approaches like the one presented in this paper.

## Acknowledgments

480 R.K. was supported for the most part of this work by a Marie Curie Fellowship under project BBfor2 from European Commission (FP7-ITN-238803). This work has also been partially supported by Spanish Guardia Civil, and project CogniMetrics (TEC2015-70627-R) from Spanish MINECO/FEDER. The researchers from Halmstad University acknowledge funding from KK-SIDUS-AIR

485 project and the CAISR program in Sweden.

## References

- [1] D. R. Ashbaugh, Quantitative-qualitative friction ridge analysis: an introduction to basic and advanced ridgeology, Boca Raton: CRC press.
- [2] V. N. Dvornychenko, D. Garrism. M, Summary of NIST latent fingerprint testing workshop. NISTIR 7377, [http://fingerprint.nist.gov/latent/ir\\_7377.pdf](http://fingerprint.nist.gov/latent/ir_7377.pdf) (2006).  
URL [http://fingerprint.nist.gov/latent/ir\\_7377.pdf](http://fingerprint.nist.gov/latent/ir_7377.pdf)
- [3] A. Sankaran, M. Vatsa, R. Singh, Latent fingerprint matching: A survey, IEEE Access 2 (2014) 982–1004. doi:10.1109/ACCESS.2014.2349879.
- 495 [4] NIST-ELFT, <http://www.nist.gov/itl/iad/ig/latent.cfm>, evaluation of latent fingerprint technologies (2013). [link].  
URL <http://www.nist.gov/itl/iad/ig/latent.cfm>

- [5] M. Indovina, R. Hicklin, *et al.*, NIST evaluation of latent fingerprint technologies: Extended feature sets [Evaluation #1], NIST Interagency/Internal Report (NISTIR) - 7775, Tech. Rep.
- [6] NIST-ELFT-1, [http://biometrics.nist.gov/cslinks/latent/elft07/phase1\\_aggregate.pdf](http://biometrics.nist.gov/cslinks/latent/elft07/phase1_aggregate.pdf), summary of the results of Phase I ELFT testing (2007). [link].  
URL <http://biometrics.nist.gov/cslinks/latent/elft07/phase1aggregate.pdf>
- [7] M. Indovina, V. Dvornychenko, *et al.*, An evaluation of automated latent fingerprint identification technology (Phase II), NIST Interagency/Internal Report (NISTIR) - 7577.
- [8] M. Indovina, V. Dvornychenko, *et al.*, Evaluation of latent fingerprint technologies: Extended feature sets (evaluation 2), NIST Technical Report, NISTIR - 7859.
- [9] A. Jain, Automatic Fingerprint Matching Using Extended Feature Set, US Department of Justice, Document NNCJ, 235577.
- [10] A. Hicklin, Standardizing a More Complete Set of Fingerprint Features, [http://fingerprint.nist.gov/STANDARD/cdeffs/Docs/IAI\\_CDEFFS\\_2007-07-24.pdf](http://fingerprint.nist.gov/STANDARD/cdeffs/Docs/IAI_CDEFFS_2007-07-24.pdf) (2007).  
URL [http://fingerprint.nist.gov/STANDARD/cdeffs/Docs/IAI\\_CDEFFS\\_2007-07-24.pdf](http://fingerprint.nist.gov/STANDARD/cdeffs/Docs/IAI_CDEFFS_2007-07-24.pdf)
- [11] E. Holder, L. Robinson, J. Laub, The Fingerprint Sourcebook, Department of Justice, Office of Justice Programs.
- [12] A. Hicklin, Extended Fingerprint Feature Set, [http://biometrics.nist.gov/cs\\_links/standard/archived/workshops/workshop2/\Presentations-docs/Hicklin-Ext-FP-Features.pdf](http://biometrics.nist.gov/cs_links/standard/archived/workshops/workshop2/\Presentations-docs/Hicklin-Ext-FP-Features.pdf) (2005).  
URL [http://biometrics.nist.gov/cs\\_links/standard/archived/workshops/workshop2/\Presentations-docs/Hicklin-Ext-FP-Features.pdf](http://biometrics.nist.gov/cs_links/standard/archived/workshops/workshop2/\Presentations-docs/Hicklin-Ext-FP-Features.pdf)
- [13] R. P. Krish, J. Fierrez, D. Ramos, Integrating rare minutiae in generic fingerprint

matchers for forensics, in: Proc. 7th IEEE Int. Workshop on Information Forensics and Security, WIFS, 2015.

- [14] M. Indovina, R. A. Hicklin, G. I. Kiebzinski, ELFT-EFS Evaluation of Latent Fingerprint Technologies: Extended Feature Sets [Evaluation# 1], National Institute of Standards and Technology, US Department of Commerce NISTIR 7775.  
530
- [15] M. Indovina, V. Dvornychenko, R. A. Hicklin, I. G. Kiebzinski, ELFT-EFS Evaluation of Latent Fingerprint Technologies: Extended Feature Sets [Evaluation# 2], National Institute of Standards and Technology, US Department of Commerce  
535 NISTIR 7859.
- [16] M. Indovina, V. Dvornychenko, R. A. Hicklin, I. G. Kiebzinski, ELFT-EFS2 Results, [http://biometrics.nist.gov/cs\\_links/latent/elft-efs/IAI\\_2012/ELFT-EFS2\\_IAI\\_2012\\_Final.pdf](http://biometrics.nist.gov/cs_links/latent/elft-efs/IAI_2012/ELFT-EFS2_IAI_2012_Final.pdf) (2012).  
URL [http://biometrics.nist.gov/cs\\_links/latent/elft-efs/IAI\\_2012/ELFT-EFS2\\_IAI\\_2012\\_Final.pdf](http://biometrics.nist.gov/cs_links/latent/elft-efs/IAI_2012/ELFT-EFS2_IAI_2012_Final.pdf)  
540
- [17] J. Fierrez-Aguilar, Y. Chen, J. Ortega-Garcia, A. K. Jain, Incorporating image quality in multi-algorithm fingerprint verification, in: Proc. IAPR Intl. Conf. on Biometrics, ICB, Vol. 3832 of LNCS, Springer, 2006, pp. 213–220.
- [18] A. Jain, J. Feng, Latent Fingerprint Matching, IEEE Transactions on Pattern Analysis and Machine Intelligence 33 (1) (2011) 88–100.  
545
- [19] Q. Zhao, A. Jain, On the utility of extended fingerprint features: A study on pores, IEEE Computer Society Conference In Computer Vision and Pattern Recognition Workshops (CVPRW) (2010) 9–16.
- [20] A. Jain, Y. Chen, M. Demirkus, Pores and ridges: High-resolution fingerprint matching using level 3 features, IEEE Transactions on Pattern Analysis and Machine Intelligence 29 (1) (2007) 15–27.  
550
- [21] Y. Chen, A. Jain, Dots and incipients: extended features for partial fingerprint matching (2007).
- [22] J. D. Stosz, L. A. Alyea, Automated System for Fingerprint Authentication Using Pores and Ridge Structure, In Proc. SPIE Conference on Automatic Systems for the Identification and Inspection of Humans 2277 (1994) 210–223.  
555

- [23] A. R. Roddy, J. D. Stosz, Fingerprint features-statistical analysis and system performance estimates, *Proceedings of the IEEE* 85 (9) (1997) 1390–1421.
- [24] K. Kryszczuk, A. Drygajlo, P. Morier, Extraction of Level 2 and Level 3 Features for Fragmentary Fingerprints, In *Proc. COST Action 275 Workshop* (2004) 83–88.
- [25] M. Vatsa, S. Richa, N. Afzel, S. K. S, Quality induced fingerprint identification using extended feature set, *IEEE International Conference in Biometrics: Theory, Applications and Systems (BTAS)* (2008) 1–6.
- [26] J. Fierrez, L. Nanni, J. Ortega-Garcia, C. R., D. Maltoni, Combining multiple matchers for fingerprint verification: a case study in FVC2000, *Proc. 13th IAPR Intl. Conf. on Image Analysis and Processing, ICIAP, Springer LNCS-3617* (2005) 035–1042.
- [27] R. P. Krish., J. Fierrez, D. Ramos, J. Ortega-Garcia, J. Bigun, Pre-Registration of Latent Fingerprints based on Orientation Field, *IET Biometrics* 4 (2) (2015) 42–52. doi:<http://dx.doi.org/10.1049/iet-bmt.2014.0087>.
- [28] R. P. Krish, J. Fierrez, D. Ramos, J. Ortega-Garcia, J. Bigun, Pre-registration for improved latent fingerprint identification, in: *Proc. IAPR/IEEE 22nd Int. Conf. on Pattern Recognition, ICPR, 2014*, pp. 696–701.
- [29] R. P. Krish, J. Fierrez, D. Ramos, J. Ortega-Garcia, J. Bigun, Partial fingerprint registration for forensics using minutiae-generated orientation fields, in: *2nd International Workshop on Biometrics and Forensics*, 2014.
- [30] X. Si, J. Feng, B. Yuan, J. Zhou, Dense registration of fingerprints, *Pattern Recognition* 63 (Supplement C) (2017) 87 – 101. doi:<https://doi.org/10.1016/j.patcog.2016.09.012>.
- [31] K. Cao, A. K. Jain, Automated latent fingerprint recognition, *CoRR* abs/1704.01925 (2017) 1–13. *arXiv:1704.01925*. URL <http://arxiv.org/abs/1704.01925>
- [32] F. Santamaria, A New Method of Evaluating Ridge Characteristics, *Fingerprint and Identification Magazine*.

- 585 [33] Neurotec-Biometric-4.3, Neurotechnology VeriFinger-SDK, <http://www.neurotechnology.com/verifinger.html>.  
URL <http://www.neurotechnology.com/verifinger.html>
- [34] F. Alonso-Fernandez, J. Fierrez-Aguilar, J. Ortega-Garcia, An enhanced gabor filter-based segmentation algorithm for fingerprint recognition systems, in: Proc. IEEE Intl. Symposium on Image and Signal Processing and Analysis, ISPA, Special Session on Signal and Image Processing for Biometrics, 2005, pp. 239–244.  
590
- [35] A. Sankaran, A. Jain, T. Vashisth, M. Vatsa, R. Singh, Adaptive latent fingerprint segmentation using feature selection and random decision forest classification, Information Fusion 34 (Supplement C) (2017) 1 – 15.  
595 doi:<https://doi.org/10.1016/j.inffus.2016.05.002>.  
URL <http://www.sciencedirect.com/science/article/pii/S1566253516300434>
- [36] E. Gutierrez-Redomero, N. Rivaldera, C. Alonso-Rodriguez, L. M. Martn, J. E. Dipierri, M. A. Fernandez-Peire, R. Morillo, Are there population differences in minutiae frequencies? a comparative study of two argentinian population samples and one spanish sample, Forensic Science International 222 (1) (2012) 266 – 276. doi:<https://doi.org/10.1016/j.forsciint.2012.07.003>.  
600 URL <http://www.sciencedirect.com/science/article/pii/S0379073812003386>
- [37] E. Gutierrez-Redomero, C. Alonso-Rodriguez, L. E. Hernandez-Hurtado, J. L. Rodriguez-Villalba, Distribution of the minutiae in the fingerprints of a sample of the spanish population, Forensic Science International 208 (1) (2011) 79 – 90. doi:<https://doi.org/10.1016/j.forsciint.2010.11.006>.  
605 URL <http://www.sciencedirect.com/science/article/pii/S0379073810005074>  
610
- [38] F. Alonso-Fernandez, J. Fierrez, J. Ortega-Garcia, J. Gonzalez-Rodriguez, H. Fronthaler, K. Kollreider, J. Bigun, A comparative study of fingerprint image-quality estimation methods, IEEE Trans. on Information Forensics and Security 2 (4) (2007) 734–743. doi:<https://doi.org/10.1109/TIFS.2007.908228>.

- 615 [39] F. Alonso-Fernandez, J. Fierrez, J. Ortega-Garcia, Quality measures in biometric systems, *IEEE Security and Privacy* 10 (9) (2012) 52–62. doi:<http://dx.doi.org/10.1109/MSP.2011.178>.
- [40] A. A. Paulino, J. Feng, A. K. Jain, Latent fingerprint matching using descriptor-based hough transform, *IEEE Transactions on Information Forensics and Security* 8 (1) (2013) 31–45.  
620
- [41] F. Zheng, C. Yang, Latent Fingerprint Match using Minutia Spherical Coordinate Code, 8<sup>th</sup> IAPR International Conference on Biometrics.
- [42] NIST-NBIS, NIST Biometric Image Software, <http://www.nist.gov/itl/iad/ig/nbis.cfm> (NBIS-Release v4.2.0).  
625 URL <http://www.nist.gov/itl/iad/ig/nbis.cfm>
- [43] R. Cappelli, M. Ferrara, D. Maltoni, Minutia Cylinder-Code: a new representation and matching technique for fingerprint recognition, *IEEE Transactions on Pattern Analysis Machine Intelligence* 32 (12) (2010) 2128–2141.
- [44] R. Cappelli, M. Ferrara, D. Maltoni, Fingerprint Indexing based on Minutia Cylinder Code, *IEEE Transactions on Pattern Analysis and Machine Intelligence* 33 (5) (2011) 1051–1057.  
630
- [45] M. Ferrara, D. Maltoni, R. Cappelli, Noninvertible Minutia Cylinder-Code Representation, *IEEE Transactions on Information Forensics and Security* 7 (6) (2012) 1727–1737.
- 635 [46] J. Fierrez, A. Morales, R. Vera-Rodriguez, D. Camacho, Multiple classifiers in biometrics. part 2: Trends and challenges, *Information Fusion* 44 (2018) 103–112. doi:<https://doi.org/10.1016/j.inffus.2017.12.005>.